



KENTUCKY CENTER
FOR MATHEMATICS

**Math Intervention
Expert Talks
with
Kristie Manley**

Kentucky Center for Mathematics

- KCM seeks to advance the knowledge and practice of effective mathematics teaching and learning, encompassing early childhood through adult education.
- KCM provides and develops statewide leadership, facilitate professional learning experiences, and cultivate innovation with the aim of improving mathematics education, practice and policy.

KCM Yearly Numbers

29 math courses taught

73 cohorts of teachers

Over 1000 KY teachers
attending

Over 182 days of
math professional learning

Over \$150,000 of math
materials directly in the hands
of teachers

109 school districts

300 KY schools

100 principals trained

>5000 students impacted

KCM Annual Math Conference
national prominence

Closing the achievement gap
for our KY math students.

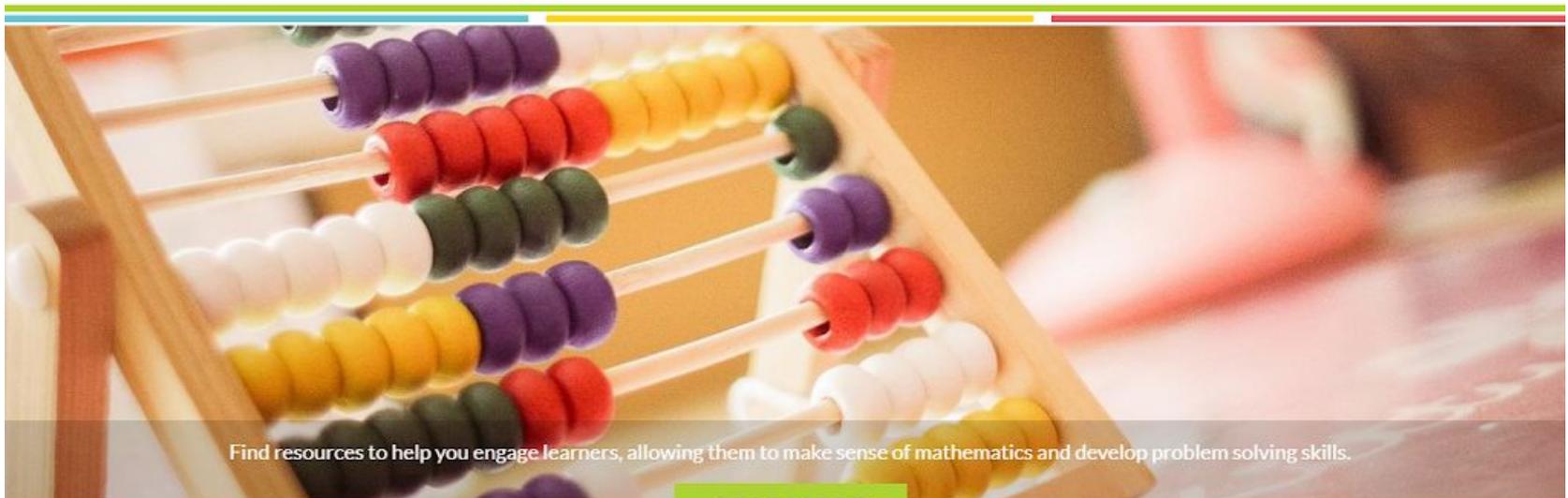
Math Achievement Fund
intervention students (3000)
had an average of 10 percentile
points gained as a direct result
of KCM trained math
interventionists.

Visit Our Website

www.kentuckymathematics.org



- HOME
- MAF
- PROFESSIONAL LEARNING ▾
- RESOURCES ▾
- ANNUAL CONFERENCE ▾
- ABOUT US ▾



Find resources to help you engage learners, allowing them to make sense of mathematics and develop problem solving skills.



Welcome!

Expert Math Interventionist

Kristie Manley

Kenwood Elementary School
Jefferson County Public Schools
Louisville, KY



kristie.manley@jefferson.kyschools.us



@kmanley0628

More About Me

- ❑ Interventionist for 3 years
- ❑ Instructional Coach for 11 years
- ❑ NBCT
- ❑ Connected to KCM for 8 years
- ❑ Crafts- wreath making, scrapbooking
- ❑ Mom of one, 8 yr old girl

KY Math Intervention



Thank You!

Kentucky legislators created the Mathematics Achievement Fund in 2005.

The goal of the MAF is...

“to provide developmentally appropriate diagnostic assessment and intervention services to students, primary through grade 12, to help them reach proficiency in mathematics on the state assessments.”

Agenda

- Bridging the Gap: Fluency to 100
- What the Research and Standards Say
- Strategies
 - Adding up to a decuple
 - Subtracting down to a decuple
- Games
 - How far away?
 - Bump it?
 - Four in a Row
- Links to Resources

What the research says...

“The ability to **flexibly decompose** numbers is foundational for using both traditional and alternative algorithms for addition, subtraction, multiplication, and division (Fuson 1990, 2003). Therefore, a **deep understanding** of place value is crucial (Hiebert and Wearne 1992), but this understanding hinges on developing ideas across K–grade 5 (Common Core Standards Writing Team 2015).”

Common Core brief: The place-value progression Temple A. Walkowiak

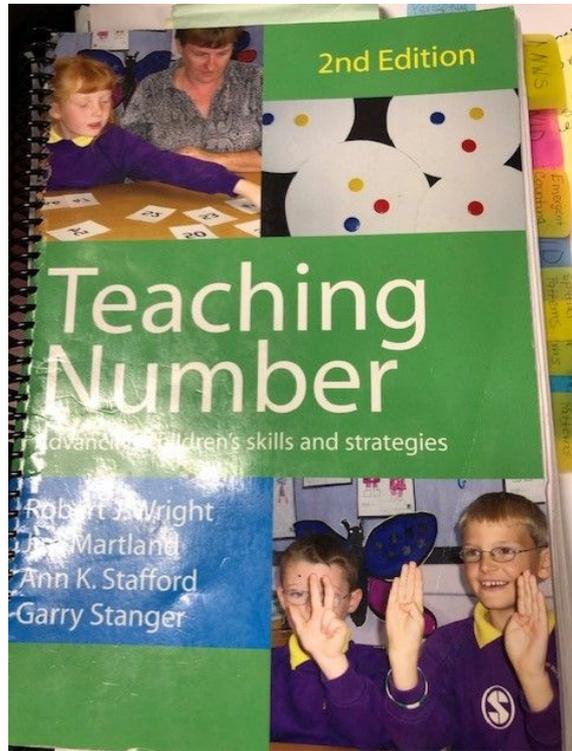
[NCTM Teaching Children Mathematics April 2016, Vol. 22, Issue 8](#)

What the research says...

“... Children develop, discuss, and use efficient, accurate, and generalizable methods to add and subtract multi digit whole numbers. They select and apply appropriate methods to estimate sums and differences or calculate them mentally, depending on the context and numbers involved. They develop fluency with efficient procedures, including standard algorithms, for adding and subtracting whole numbers, understand **why the procedures work** (on the basis of place value and properties of operations), and use them to solve problems. (NCTM 2006, p. 14)”

Addition and Subtraction: The Big Ideas and Essential Understandings,
NCTM pdf- in handouts

Research



KCM

KENTUCKY CENTER
FOR MATHEMATICS



Standards

KY.1.OA.6 Add and subtract within 20. a. Fluently add and subtract within 10. b. Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making 10; decomposing a number leading to a 10; using the relationship between addition and subtraction; creating equivalent but easier or known sum

KY.2.OA.2 Fluently add and subtract within 20 using mental strategies.
MP.2, MP.7, MP.8

KY.2.NBT.5 Fluently add and subtract within 100 using strategies based on place value, properties of operations and/or the relationship between addition and subtraction.

Stages of Early Arithmetic Learning (SEAL)

(Steffe et al. 1988; Steffe 1992; Wright et al. 2006*)

A framework for
Interpreting Student's
Counting, Addition and
Subtraction Strategies

[Pathways to Number Link](#)



* Steffe, Leslie. 1992. "Learning Stages in the Construction of the Number Sequence." In *Pathways to Number: Children's Developing Numerical Abilities*, edited by Jacqueline Bideaud, Claire Meljac, and Jean-Paul Fischer, pp. 83–88. Mahwah, NJ: Lawrence Erlbaum Associates.

Steffe, Leslie P., Paul Cobb, and Ernst von Glasersfeld. 1988. *Construction of Arithmetical Meanings and Strategies*. New York: Springer-Verlag.

Wright, Robert J., James Martland, and Ann Stafford. 2006. *Early Numeracy: Assessment for Teaching and Intervention*. 2nd ed. London: Paul Chapman Publications/Sage.

Developing Qualities

Use these descriptions of diagnostic and instructional tools to help young learners move beyond reliance on physical materials to negotiate arithmetic tasks.



By Jonathan N. Thomas
and Pamela D. Tabor

Joseph is a first-grade student whose teacher is working to better understand the manner in which he approaches the following exchange around the task $11 + 4$.

By Jonathan N. Thomas
and Pamela D. Tabor

Mental Imagery

Each new phase in the Stages of Early Arithmetic Learning (SEAL) model incorporates, rather than displaces, the knowledge and understanding of prior stages.

Stages of Early Arithmetic Learning (SEAL)
(Steffe et al. 1988; Steffe 1992; Wright et al. 2006)

Emergent

Child approximates counting activity (e.g., saying number words when asked, “How many?”) but is typically unable to determine the numerosity of a collection.

What it might look like: Child is presented with a collection of twelve counters and asked how many are there. Child touches some, but not all, the counters, saying, “One, two, three, five, seven, eight, nine—nine!”

Hallmark strategy: Attempting to count a collection

Perceptual

Child can determine the numerosity of collections when physical materials are available for counting but is unable to negotiate arithmetic tasks in the absence of physical materials.

What it might look like: Child is presented with collections of nine counters and five counters and asked, “How many altogether?” The child touches each of the counters while saying, “One, two, three, four, five, six, seven, eight, nine, ten, eleven, twelve, thirteen, fourteen!”

Hallmark strategy: Physically interacting with materials to count collections

Figurative

Child can negotiate arithmetic tasks in the absence of physical materials by generating mental imagery of past sensory experiences referred to as *re-presentations*.

What it might look like: Child is presented with a collection of nine counters and five counters; the counters are then concealed. Child is asked how many altogether. The child looks away, begins counting at one (may or may not sequentially raise fingers), and says, “One, two,

three, four, five, six, seven, eight, nine, ten, eleven, twelve, thirteen, fourteen—fourteen!”

Hallmark strategy: Continuing the count from one when materials are physically unavailable

Initial number sequence

Child can negotiate arithmetic tasks in the absence of physical materials by constructing a single chunk of a number, referred to as a *numerical composite*, and then counting on from this chunk.

What it might look like: Child is presented with collections of nine and five counters, and the counters are then concealed. Child is asked how many altogether. Child counts on from nine (may or may not sequentially raise fingers) and says, “Ten, eleven, twelve, thirteen, fourteen—fourteen!”

Hallmark strategy: Counting on when materials are physically unavailable

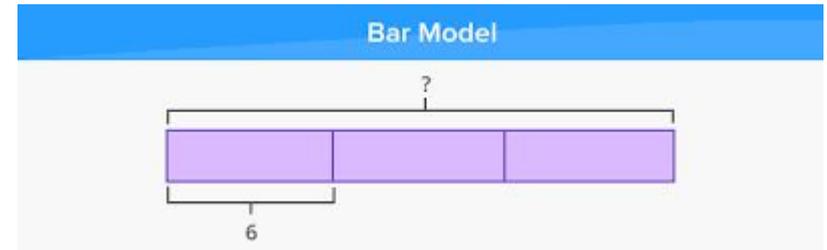
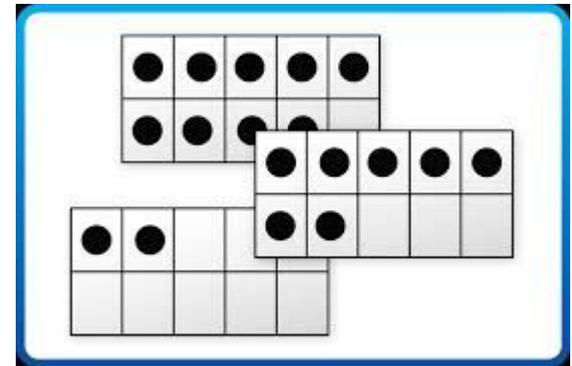
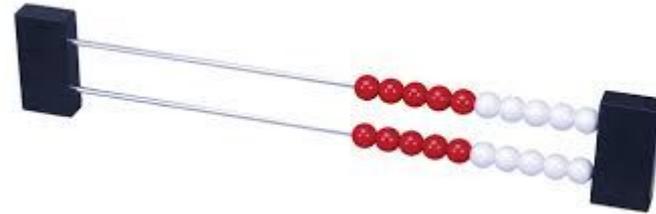
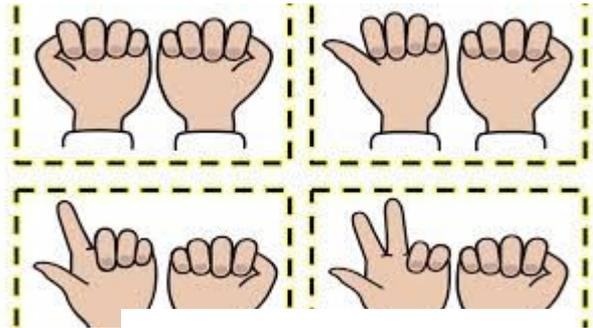
Facile number sequence

Child can negotiate arithmetic tasks in the absence of physical materials by constructing multiple chunks of numbers, referred to as *abstract numerical composites*, and decomposing/recomposing these chunks.

What it might look like: Child is presented with collections of nine and five counters, and the counters are then concealed and asked how many altogether. The child responds immediately, “Fourteen—I borrowed one from the five to make ten, and then just added ten and four in my head.”

Hallmark strategy: Multiple non-count-by-ones strategies when materials are physically unavailable

What is structure?



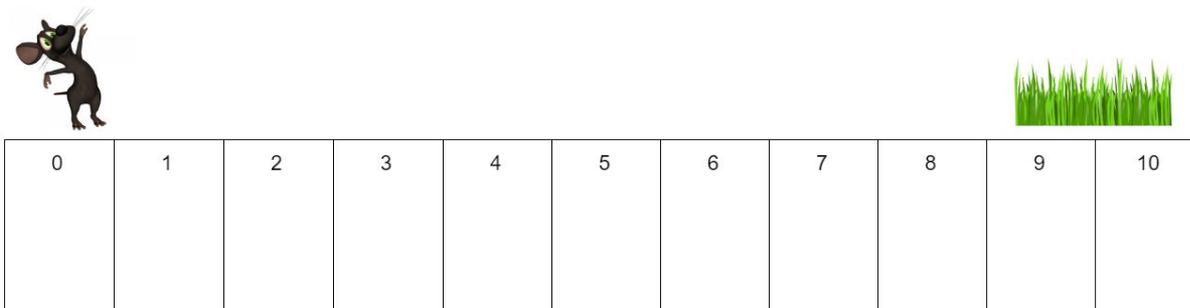
Adding up to a Decade



Subtracting down to a Decade



How far away?



You can use this for adding up to a decuple or subtracting down to a decuple.

Students will roll place value dice and then determine how far to the next decuple. First person to cover their path wins.

Bump It

Need Place value dice

Counters (two colors)

Materials for support

How to Play:

P1 rolls the dice. They create a 2 digit number. They then determine how many more to the next decuple. That is the number they cover on the board. P2 does the same. If all the numbers of the answer are covered, then the player may “bump” their opponent. Players are trying to get 4 in a row.

BUMP IT
Adding to a decuple

1	9	6	3	2
7	2	1	3	1
8	4	3	9	2
5	3	8	4	9
1	7	6	4	5
6	5	2	7	8

<https://myfreebingocards.com/bingo-card-generator>

4 in a Row

P1 will either spin a spinner or roll place value dice to get a 2 digit number. Then subtract down to the previous decuple. How many they subtract down is what they cover. The goal is to get 4 in a row.

Four -in- a -Row
Subtracting to a decuple

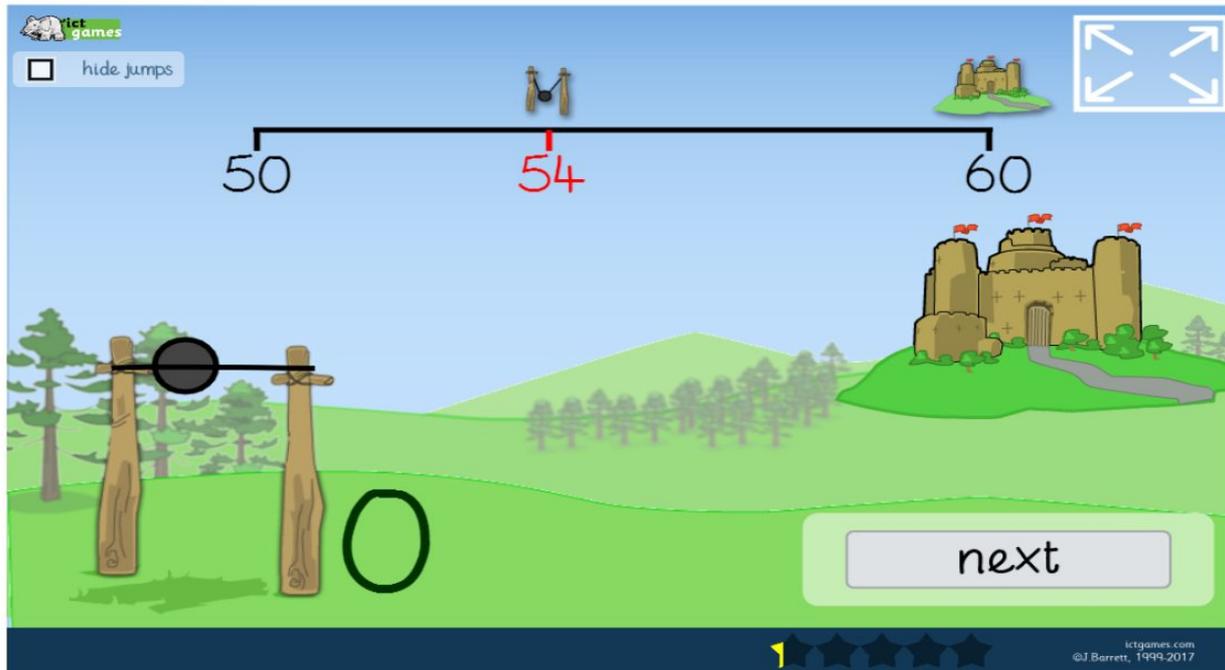
1	9	6	3	2
7	2	1	3	1
8	4	3	9	2
5	3	8	4	9
1	7	6	4	5
6	5	2	7	8

Handouts

- ❑ How far away?
- ❑ Bump it
 - adding up to a decuple
 - subtracting down to a decuple
 - partners of 5
 - small and large partners of 10
 - NWA teen numbers
 - Crossing the decade (29 to 30)
- ❑ Four-in-a-Row
 - adding up to a decuple
 - subtracting down to a decuple
 - partners of 5
 - NWB within 100
 - Partners of 10
 - Number Id 1-5
 - NWA within teen numbers
- ❑ ten frame cards (2 sets)
- ❑ dot strips

Virtual Option

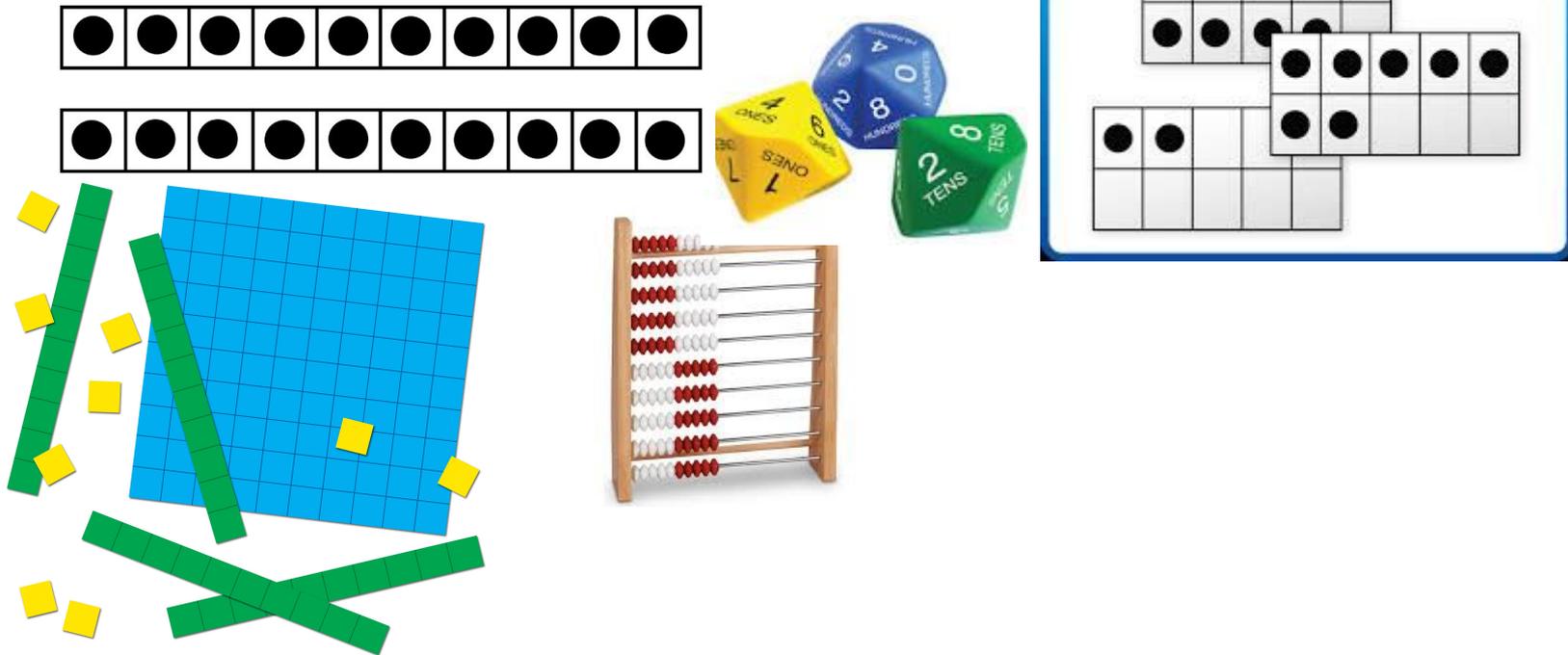
<https://www.ictgames.com/mobilePage/catapultCountOn/index.html>



Materials to have on hand.....

<https://www.coolmath4kids.com/manipulatives/base-ten-blocks>

<https://toytheater.com/rekenrek-ten-rows/>



Visit Our KCM Website

www.kentuckymathematics.org



GOOD NEWS

KCM Launches Multi-Series Virtual PD

Find out more in this month's article!



Good News!

The KCM is hard at work to ensure Kentucky teachers have access to innovative professional development from home.

Through the newly launched [KCM Virtual](#) site, mathematics teachers from all grade levels will have access to live zoom meetings, video records and corresponding materials. [Read more.](#)

[Elementary: Make 'n Take Supporting Number Sense and Fluency - Mar. 23-27](#)

[Middle: Fractions, Decimals & Percents - Mar. 30-Apr. 3](#)

[High: Algebra & Geometry - Thursdays, Mar. 26 - Apr. 16](#)

[Math Intervention Expert Talks - Apr. 6 - Apr. 10](#)

[Focus on Place Value - Apr. 13 - Apr. 17](#)

Upcoming Virtual Professional Learning

APRIL 6 - 10
2:00-2:30 PM EST



Math Intervention Expert Talks!

w/ KY Math Leaders

Monday, April 6 - Meet the Expert- Kristie Manley

Tuesday, April 7 - Instructional Moves with KCM's Lisa Riggs

Wednesday, April 8 - Meet the Expert- Michael Hines

Thursday, April 9 - Instructional Moves with KCM's Tonda Thompson

Friday, April 10 - Meet the Expert- Jackie Damron

KCM is here to support teachers!

Expert Math Interventionist



Kristie Manley

Kenwood Elementary School
Jefferson County Public Schools
Louisville, KY



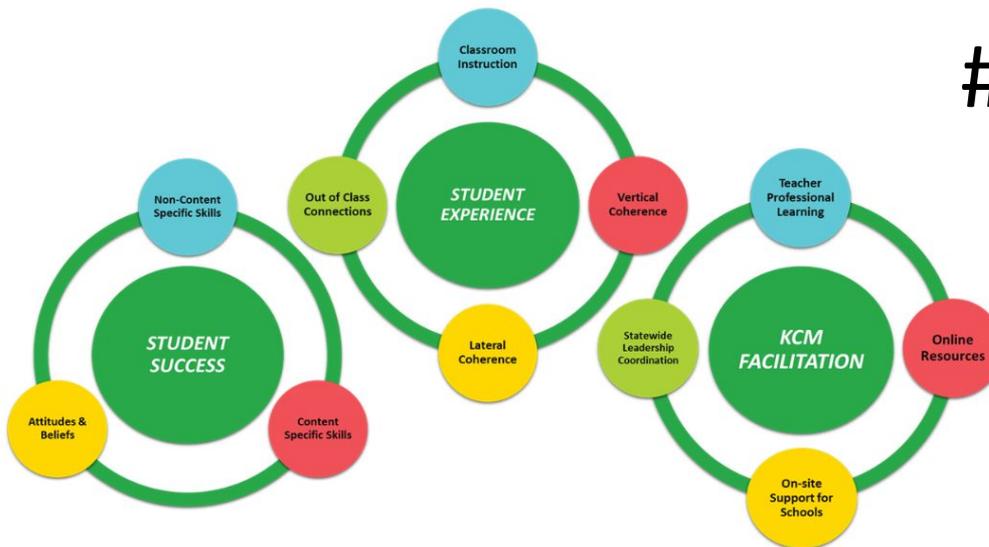
kristie.manley@jefferson.kyschools.us



@kmanley0628

KCM Support for Educators

- Kentucky Center for Mathematics is here to support our KY educators
- We aspire to be a national leader in mathematics education



#BetterTogether
#TeamKCM